

Antenna Parameters

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1 Radiation Fields

The radiation fields are actually just the E-field and H-field of the antenna.

For example, $E_{Hertzian} = \frac{\eta j k I \Delta z e^{-jkr}}{4\pi r} \left[1 + \frac{1}{jkr} + \frac{1}{(jkr)^2} \right] \sin \theta \hat{\theta}$, expand it

$$E_{Hertzian} = \left[\underbrace{\frac{\eta j k I \Delta z e^{-jkr}}{4\pi r}}_{\text{Radiation term}} + \underbrace{\frac{\eta I \Delta z e^{-jkr}}{4\pi r^2}}_{\text{Induction term}} + \underbrace{\frac{\eta I \Delta z e^{-jkr}}{4j\pi k r^3}}_{\text{Electrostatic term}} \right] \sin \theta \hat{\theta}$$

Certain approximation is needed to handle the complicated field

When r is large, the radiation term dominant.

When r is large, the electrostatic term dominant.

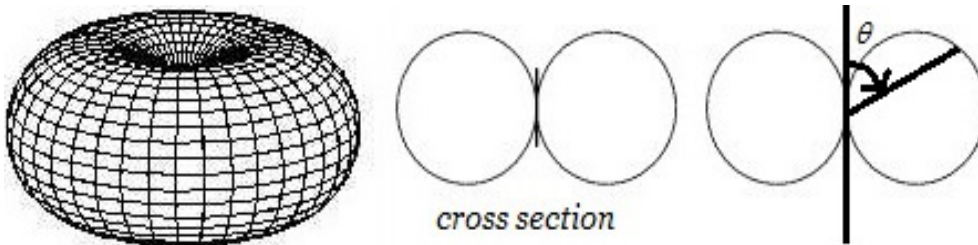
Thus, for *Far Field* ($kr \gg 1$), $E_{Hertzian} \approx E_{Rad}$

$$E_{FarField} = \frac{\eta j k I \Delta z e^{-jkr}}{4\pi r} \sin \theta \cdot \hat{\theta} \quad H_{FarField} = \frac{j k I \Delta z e^{-jkr}}{4\pi r} \sin \theta \cdot \hat{\phi}$$

The fields $E \perp H$, and

$$|E_{FarField}| = \frac{\eta k |I| |\Delta z e^{-jkr}| \sin \theta}{4\pi r} \quad |H_{FarField}| = \frac{k |I| |\Delta z e^{-jkr}| \sin \theta}{4\pi r}$$

It looks like



For the above diagram, notice that when $\theta = 90$ (sin achieve its maximum)

2 Power Terms

The Poynting Vector $\bar{S} = \bar{E} \times \bar{H}$ can be used for power manipulation.

The time-dependent Poynting Vector $\bar{S}(r, t) = \bar{E}(r, t) \times \bar{H}(r, t)$

The time-average Poynting Vector $\langle \bar{S}(r) \rangle = \frac{1}{2} \text{Re} [\bar{E}(r) \times \bar{H}(r)^*]$

The Total radiated power $P_{Rad} = \iint_S \langle \bar{S}(r) \rangle \cdot d\mathbf{S} = \int_{\phi=0}^{\phi=2\pi} \int_{\theta=0}^{\theta=\pi} \langle \bar{S}(r) \rangle \cdot \hat{r} r^2 \sin \theta d\theta d\phi$

Average radiated power $P^{Avg} = \frac{P_{Rad}}{\iint_S dS} = \frac{P^{Tot}}{4\pi r^2}$

3 Antenna Gain and Directivity

$$G = \frac{\langle \bar{S}(r) \rangle}{P^{Avg}} = \frac{\langle \bar{S}(r) \rangle}{P_{Rad}/4\pi r^2}$$

Directivity $D = \max G$

4 Antenna Circuit Equivalent

$$\text{Radiation Resistance } R_{Rad} = \frac{P_{Rad}}{I_{Rms}^2}$$

$$\text{Radiation Efficiency } Eff_{Rad} = \frac{R_{Rad}}{R_{Rad} + R_{OhmicLoss}}$$

Input Impedance $Z_{In(Rad)} = R_{Rad} + \chi_{Circuit} + R_{Ohmic}$

$$\text{Effective Length } l_{Eff} = \underbrace{\int_{-\frac{l}{2}}^{+\frac{l}{2}} I(z) dz}_{Tx} = \underbrace{\frac{V_{OC}}{|E_{Receiving}|}}_{Rx}$$

Power deliver to matched load for lossless antenna $P_L = \frac{1}{2} \left(\frac{V_{OC}^2}{4R_{Rad}} \right)$

$$\text{Effective Area for Rx } A_{Eff} = \frac{P_L}{P_{\text{incident EM}}} = \frac{\lambda^2}{4\pi} G$$

$$\text{Friis Transmission Formula } \frac{P_L}{P_{Rad(Tx)}} = \frac{A_{EffTx} A_{EffRx}}{r^2 \lambda^2} = \frac{D_{Tx} D_{Rx} \lambda^2}{(4\pi r)^2}$$

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